



**PRESIDENCY UNIVERSITY
BENGALURU**

SCHOOL OF ENGINEERING

TEST 1

Seme & AY: Odd Sem. 2019-20

Course Code: ECE 307

Course Name: DIGITAL IMAGE PROCESSING

Program & Sem: B.Tech (ECE) & V DE

Date: 27.09.2019

Time: 2.30PM to 3.30PM

Max Marks: 40

Weightage: 20%

Instruction:

- (i) Read the question properly and answer accordingly.
- (ii) Question paper consists of 3 parts.
- (iii) Scientific and Non-programmable calculators are permitted.

Part A [Memory Recall Questions]

Answer all the Questions. Each Question carries one marks. (10Qx1M=10M)

1. If R is a subset of pixels, we call R a _____ of the image if R is a connected set.
(C.O.NO.1) [Knowledge]
(a) Disjoint (b) Region (c) Closed (d) Adjacent

2. The distance between pixels p and q, the pixels have a distance less than or equal to some value of radius r, form a diamond centred at (x,y) is called :
(C.O.NO.1) [Knowledge]
(a) Euclidean distance (b) Chessboard distance
(c) City-Block distance (d) None of the Mentioned

3. A pixel "p" at coordinates (x, y) has neighbors whose coordinates are given by: (x+1, y+1), (x+1, y-1), (x-1, y+1), (x-1, y-1) .This set of pixels is called _____
(C.O.NO.1) [Knowledge]
(a) 4-neighbors of p (b) Diagonal neighbors
(c) 8-neighbors (d) None of the mentioned

4. In terms of Sampling and Quantization, Zooming and Shrinking may be viewed as ____
(C.O.NO.1) [Knowledge]
(a) Oversampling for both
(b) Undersampling for both
(c) Undersampling & Oversampling respectively
(d) Oversampling & Undersampling respectively

5. After digitization process a digital image with M rows and N columns have to be positive and for the number, L, max gray levels i.e. an integer power of 2 for each pixel. Then, the number b, of bits required to store a digitized image is: (C.O.NO.1) [Knowledge]
 (a) $b=M*N*k$ (b) $b=M*N*L$ (c) $b=M*L*k$ (d) $b=L*N*k$
6. Which is a colour attribute that describes a pure colour? (C.O.NO.1) [Knowledge]
 (a) Saturation (b) Hue (c) Brightness (d) Intensity
7. To convert a continuous image $f(x, y)$ to digital form, we have to sample the function in _____ (C.O.NO.1) [Knowledge]
 (a) Coordinates (b) Amplitude (c) All of the mentioned
 (d) None of the mentioned
8. How many number of steps are involved in image processing? (C.O.NO.1) [Knowledge]
 (a) 12 (b) 9 (c) 11 (d) 10
9. While implementing logic operation on gray-scale images, the processing of pixel values is done as _____ (C.O.NO.1) [Knowledge]
 (a) String of integer numbers (b) String of floating numbers
 (c) String of binary numbers (d) None of the mentioned
10. Which of the following is more commercially successful image enhancement method in mask mode radiography, an area under medical imaging? (C.O.NO.1) [Knowledge]
 (a) Addition (b) Subtraction (c) Multiplication (d) Division

Part B [Thought Provoking Questions]

Answer all the Questions. Each Question carries five marks. (3Qx5M=15M)

11. Define the following: (C.O.NO.1) [Knowledge]
 (i) Image Transformation (ii) Unitary Matrix
 (iii) Orthogonal basis function (iv) Orthonormal basis function
12. Discuss the relationship between Neighbors of pixels $P(x,y)$: (C.O.NO.1) [Comprehension]
 (i) $N_4(P)$ (ii) $N_D(P)$ (iii) $N_8(P)$

?	?	?
?	$P(x,y)$?
?	?	?

13. Discuss 4-adjacency, 8-adjacency and m-adjacency. (C.O.NO.1) [Comprehension]

Part C [Problem Solving Questions]

Answer all the Questions. Each Question carries five marks. (3Qx5M=15M)

14. An image segment F1 and F2 are given : $F1 = \begin{matrix} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \end{matrix}$ and $F2 = \begin{matrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 0 & 1 \end{matrix}$,
perform

- (i) $X1 = \text{NOT } F1$ (ii) $X2 = F1 \text{ AND } F2$ (iii) $X3 = F1 \text{ OR } F2$ (iv) $X4 = F1$
XOR F2
(v) $X5 = F1 \text{ AND NOT}(F2)$

(C.O.NO.1)[Comprehension]

15. (a) Calculate the number of bits required to store a binary image, a gray image and color image of size 1024 X 1024

(b) Compute Eculidean distance (De) for points P(3,2,3) and Q(2,3,7).

(C.O.NO.1) [Comprehension]

16. An image segment A1 and A2 are given : $A1 = \begin{matrix} 7 & 11 & 30 \\ 24 & 8 & 15 \\ 18 & 14 & 10 \end{matrix}$ and $A2 = \begin{matrix} 4 & 6 & 8 \\ 1 & 3 & 7 \\ 9 & 2 & 5 \end{matrix}$,

perform array operations such as addition, subtraction and multiplication.

(C.O.NO.1) [Comprehension]



**PRESIDENCY UNIVERSITY
BENGALURU**

SCHOOL OF ENGINEERING

TEST – 1

Semester: V

Course Code: ECE307

Course Name: Digital Image Processing

Program & Sem: B.Tech/ ECE/ 5th Sem

Date: 27-09-2019 (Friday)

Time: 2.30 PM to 3.30 PM

Max Marks: 40

Weightage: 20%

Extract of question distribution [outcome wise & level wise]

Q.NO.	C.O.N O	Unit/Module Number/Unit /Module Title	Memory recall type [Marks allotted] Bloom's Levels		Thought provoking type [Marks allotted] Bloom's Levels			Problem Solving type [Marks allotted]			Total Marks
			K		C			A			
1 to 10	1	Module1		1x10							10 marks
11	1	Module2		5							5 marks
12	1	Module1				5					5 marks
13	1	Module1				5					5 marks
14	1	Module1				5					5 marks
15	1	Module1				5					5 marks
16	1	Module1				5					5 marks
	Total Marks			15		25					40 marks

K = Knowledge Level C = Comprehension Level, A = Application Level

Note: While setting all types of questions the general guideline is that about 60% Of the questions must be such that even a below average students must be able to attempt, About 20% of the questions must be such that only above average students must be able to attempt and finally 20% of the questions must be such that only the bright students must be able to attempt.

I here certify that All the questions are set as per the above lines Natya S]

Re-Check Q11,
Q12
[Signature]

[Signature] 23/09/19



**PRESIDENCY UNIVERSITY
BENGALURU**

SCHOOL OF ENGINEERING

TEST – 1

Semester: V

Course Code: ECE307

Course Name: Digital Image Processing

Program & Sem: B.Tech/ ECE/ 5th Sem

Date: 27-09-2019 (Friday)

Time: 2.30 PM to 3.30 PM

Max Marks: 40

Weightage: 20%

Part A

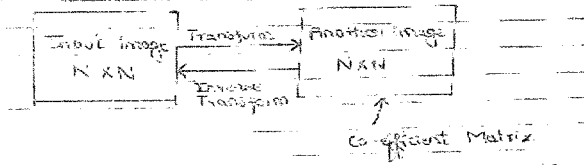
(10Q x 1M = 10Marks)

Q. No.	Solution	Scheme of Marking	Max. Time required for each Question
1.	(b) Region	1	1 min
2.	(c) City-Block distance	1	1 min
3.	(b) Diagonal neighbors	1	1 min
4.	(d) Oversampling & Undersampling respectively	1	1 min
5.	(a) $b=M*N*k$	1	1 min
6.	(b) Hue	1	1 min
7.	(a) Coordinates	1	1 min
8.	(d) 10	1	1 min
9.	(c) String of binary numbers	1	1 min
10.	(b) Subtraction	1	1 min

Part B

(3Q x 5M = 15Marks)

Q. No	Solution	Scheme of Marking	Max. Time required for each Question
11.	(i) Image Transformation	2+1+2=5M	10 Min



A function or operation that takes an image as its input & produces another image as its output.
 A linear transformation can be applied to an image to convert it from one domain to another domain.
 E.g. Discrete cosine transform, Discrete Fourier transform, KL transform, Hartley transform, Walsh transform, Hadamard transform, etc.

Applying transform we get another image of same size.
 After applying inverse transform we get the original image back.

(ii) Unitary Matrix

A matrix "A" is said to be a unitary matrix if inverse of A is equal to A star transpose where A star is the complex conjugate of A.

$$A^{-1} = A^{*T}$$

(iii) Orthogonal basis function and

(iv) Orthonormal basis function

Eg 1

Case 1-0 special:

Consider a set of real valued continuous functions
to add to be orthogonal over an interval T if

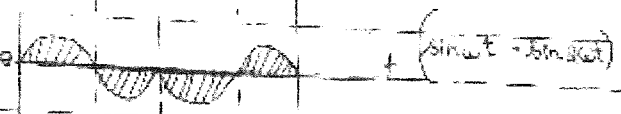
$$\int a_m(t) \cdot a_n(t) dt = \begin{cases} K & m=n \\ 0 & m \neq n \end{cases}$$

where $a_n(t) = \{a_1(t), a_2(t), \dots\}$

If the value of K is equal to 1 then the set
is orthonormal.

Eg 2 $a_n(t) = \{\sin \omega t, \sin 2\omega t\}$ over an interval
 $T = 0 \text{ to } T$

$$\int \sin \omega t \cdot \sin 2\omega t dt = 0$$



$$\int_0^T \sin \omega t \cdot \sin 2\omega t dt$$

12.

Neighbors of a pixel:

A pixel p at co-ordinates (x, y) has 4 horizontal & 4 vertical neighbours with co-ordinates $(x+1, y)$, $(x-1, y)$, $(x, y+1)$, $(x, y-1)$.
The above set of pixels are called as the 4-neighbors of a pixel p denoted by $N_4(p)$.

Some of the neighbors of a pixel p lie outside the digital image if (x, y) lies on the border of the image.



Fig: 4-neighbors of pixel p
 $N_4(p)$

A pixel p at co-ordinates (x, y) has 4 diagonal neighbours having co-ordinates $(x+1, y+1)$, $(x-1, y+1)$, $(x-1, y-1)$, $(x+1, y-1)$.
The diagonal neighbours are denoted by $N_2(p)$.

Some of the pixels in $N_2(p)$ and $N_4(p)$ may also lie outside the digital image if (x, y) is on the border of the image.

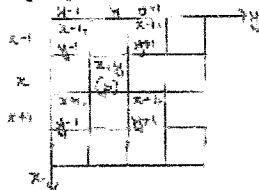


Fig: 4-Diagonals of pixel p
 $N_2(p)$

4-neighbors & 4-diagonal-neighbors are together called as 8-neighbors of a pixel p denoted by $N_8(p)$.

2+2+1=5M

10 Min

13.

Adjacency, Connectivity, Regions & Boundaries:

Let V be a set of gray-level values (intensity values) $V = \{i\}$ if we are referring to adjacency of pixels with value i in a binary image. (Binary image has only 2 gray levels 0 & 1). In a gray scale image set V can have a number of elements i.e. 0-255 if the gray levels are used.

There are 3 types of adjacency

- 1. 4-Adjacency
- 2. 8-Adjacency
- 3. M-Adjacency (mixed 8-adjacency)

4-Adjacency:

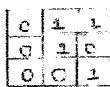
Two pixels p & q are 4-adjacent if they are adjacent horizontally or vertically.
If p & q are at $N_4(p)$ $\{p, q \in V \wedge q \in N_4(p)\}$

8-Adjacency:

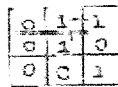
Two pixels p & q are 8-adjacent if they are adjacent horizontally, vertically or diagonally.
If p & q are at $N_8(p)$ $\{p, q \in V \wedge q \in N_8(p)\}$

M-Adjacency: (Masks multiple path connections and hence defines the boundaries)
Two pixels p & q are M-adjacent if

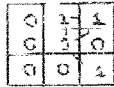
- 1. q is in $N_4(p)$ (0)
- 2. q is in $N_8(p)$ if the set $N_4(p) \cap N_8(q)$ has no pixels whose value are from V $\{q \in N_8(p) \wedge N_4(p) \cap N_8(q) = \emptyset\}$



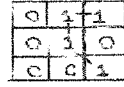
1. 4-adjacency of pixels



2. 8-adjacency



3. M-adjacency



4. M-adjacency

$V = \{1\}$

1+1+1+2=5M

10 Min

Part C

(3Q x 5M = 15Marks)

Q.No	Solution	Scheme of Marking	Max. Time required for each Question
14.	$\begin{matrix} 0 & 1 & 0 \\ X1= & 0 & 0 & 0 \\ & 1 & 0 & 1 \\ \\ & 1 & 0 & 1 \\ X2= & 1 & 1 & 0 \\ & 0 & 0 & 0 \\ \\ & 1 & 1 & 1 \\ X3= & 1 & 1 & 1 \\ & 0 & 1 & 1 \\ \\ & 0 & 1 & 0 \\ X4= & 0 & 0 & 1 \\ & 0 & 1 & 1 \\ \\ & 0 & 0 & 0 \\ X5= & 0 & 0 & 1 \\ & 0 & 1 & 0 \end{matrix}$	1x5=5M	5 min
15. (a)	<p><u>Sol:</u></p> <p>(i) For a binary image 1 bit is sufficient for representing a pixel value. \therefore No. of bits required = $1024 \times 1024 \times 1$ = <u>1,048,576 bits</u></p> <p>(ii) For a gray image 8 bits are required for representing a pixel value. \therefore No. of bits required = $1024 \times 1024 \times 8$ = <u>8,398,608 bits</u></p> <p>(iii) For a colour image (24 bits) RGB are required for representing a pixel value. \therefore No. of bits required = $1024 \times 1024 \times 24$ = <u>25,165,824 bits</u></p>	1+1+1=3M	5 min
15. (b)	<p><u>Euclidean distance:</u></p> $\begin{aligned} D_1 &= \sqrt{(x-10)^2 + (y-8)^2 + (z-10)^2} \\ &= \sqrt{(3-10)^2 + (2-8)^2 + (7-10)^2} \\ &= \sqrt{49 + 36 + 9} \\ &= \sqrt{94} = \underline{9.7} \end{aligned}$	1+1=2M	5 min

16.	<p>14 17 38 Addition= 25 11 22 27 16 15</p> <p>3 5 22 Subtraction= 23 5 8 9 12 5</p> <p>28 66 240 Multiplication= 24 24 105 162 28 50</p>	1.5+1.5+2=5M	5 min
-----	---	--------------	-------

Roll No.



**PRESIDENCY UNIVERSITY
BENGALURU**

SCHOOL OF ENGINEERING

TEST – 2

Sem & AY: Odd Sem 2019-20

Date: 16.11.2019

Course Code: ECE 307

Time: 2.30 PM to 3.30 PM

Course Name: DIGITAL IMAGE PROCESSING

Max Marks: 40

Program & Sem: B.Tech (ECE) & V

Weightage: 20%

Instruction:

- (i) Read the question properly and answer accordingly.
- (ii) Question paper consists of 3 parts.
- (iii) Scientific and Non-programmable calculators are permitted.

Part A [Memory Recall Questions]

Answer all the Questions. Each sub question carries one mark.

(10Qx1M=10M)

1. Fill in the blanks with correct answers

(C.O.NO.2) [Knowledge]

- a) In bit plane slicing, a 512 level gray scale image will have _____ number of 1-bit planes.
- b) A plot of $p(r_k)$ versus r_k is called _____.
- c) The general form of log transformation is $s =$ _____.
- d) The negative of a 2×2 image with pixel values $\begin{matrix} 0 & 4 \\ 3 & 6 \end{matrix}$ is _____.
- e) In cathode ray tube (CRT) devices, if γ (gamma) = 2.5, the display system would produce images that are _____ in appearance.
- f) If the components of the histogram are concentrated on lower side of the intensity scale then the image looks _____ in appearance
- g) The process of highlighting masses of water in satellite imagery and enhancing flaws in X-ray images is called _____.
- h) If input image intensities $r_1=r_2$ and output intensities $s_1=0, s_2=L-1$, this creates a binary image, this type of transformation is called _____.
- i) The basic filtering equation in frequency domain is given by _____.
- j) The frequency domain procedure for improving the appearance of an image based on illumination reflectance model is _____.

Part B [Thought Provoking Questions]

Answer all the Questions. Each Question carries five marks.

(3Qx5M=15M)

- (C.O.NO.2) [Comprehension]
2. Explain the model of image degradation/ restoration process with relevant equations.
(C.O.NO.2) [Comprehension]
 3. List the steps for filtering in frequency domain.
(C.O.NO.2) [Comprehension]
 4. Define bit plane slicing. For a given image, perform bit plane slicing.

$$\begin{bmatrix} 4 & 3 & 2 & 1 \\ 3 & 1 & 2 & 4 \\ 5 & 1 & 6 & 2 \\ 2 & 3 & 5 & 6 \end{bmatrix}$$

Part C [Problem Solving Questions]

Answer all the Questions. Each Question carries five marks.

(3Qx5M=15M)

- (C.O.NO.2) [Comprehension]
5. For a 3 bit 4*4 size image $f(x,y)$ given below, perform the following operations
 - a) Thresholding with $T=4$.
 - b) Intensity level slicing with background and without background. The range of interest of intensity values is $r1=3$ and $r2=5$.

$$f(x,y) = \begin{bmatrix} 1 & 2 & 3 & 0 \\ 2 & 4 & 6 & 7 \\ 5 & 2 & 4 & 3 \\ 3 & 2 & 6 & 1 \end{bmatrix}$$

- (C.O.NO.2) [Comprehension]
6. Consider a gray scale image in matrix form, perform histogram equalization on this image and scale the intensity to 1:20.

$$\begin{bmatrix} 3 & 2 & 4 & 5 \\ 7 & 7 & 8 & 2 \\ 3 & 1 & 2 & 3 \\ 5 & 4 & 6 & 7 \end{bmatrix}$$

- (C.O.NO.2) [Comprehension]
7. Consider a triangle with vertices $(0,0)$, $(1,0)$, $(1,1)$. This triangle is rotated 90 degrees clockwise, draw the original location of this triangle and also the new transformed figure with coordinates.



SCHOOL OF ENGINEERING

Semester: 5

Course Code: ECE307

Course Name: **DIGITAL IMAGE PROCESSING**

Date: 16/11/2019

Time: 2:30 PM TO 3:30 PM

Max Marks: 40

Weightage: 20%

Extract of question distribution [outcome wise & level wise]

Q.NO	C.O.NO	Unit/Module Number/Unit /Module Title	Memory recall type			Thought provoking type			Problem Solving type			Total Marks	
			[Marks allotted]	Bloom's Levels		[Marks allotted]	Bloom's Levels		[Marks allotted]				
			K			C			C				
1a - j	C.O.2	Module 2 (10 Objective Type Questions)	10									10	<i>Q.P Says Comp List</i>
2-4	C.O.2	Module2 and 3(Subje ctive Type Questions)				5	5	5				15	
5-7	C.O.2	Module2(Subje ctive Type Questions)							5	5	5	15	
	Total Marks			10			15			15		40	

K = Knowledge Level C = Comprehension Level, A = Application Level

Note: While setting all types of questions the general guideline is that about 60%

Of the questions must be such that even a below average students must be able to attempt, About 20% of the questions must be such that only above average students must be able to attempt and finally 20% of the questions must be such that only the bright students must be able to attempt.



Annexure- II: Format of Answer Scheme



SCHOOL OF ENGINEERING

SOLUTION

Semester: 5

Course Code: ECE307

Course Name: **DIGITAL IMAGE PROCESSING**

Date: 16/11/2019

Time: 2:30PM TO 3:30PM

Max Marks: 40

Weightage: 20

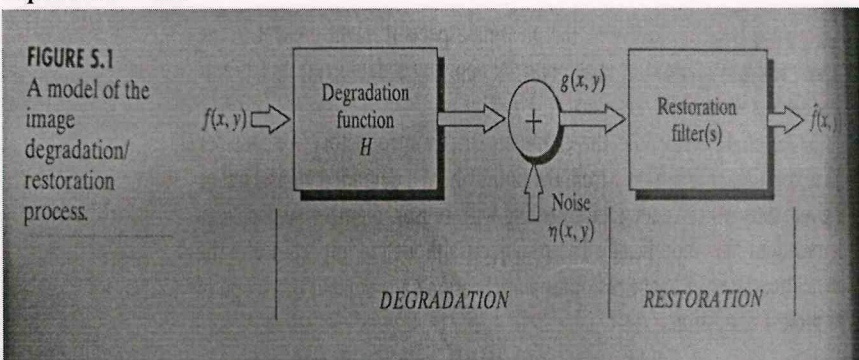
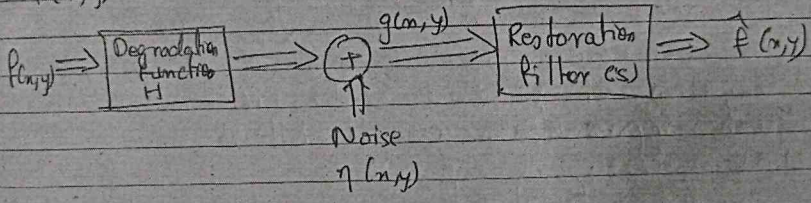
Part A

(10Q x 1M =10 Marks)

Q No	Solution	Scheme of Marking	Max. Time required for each Question
1A	9	1 Mark	1 MIN
B	Normalized histogram of input image	1 Mark	1 MIN
C	$s = c \log(1+r)$	1 Mark	1 MIN
D	$\begin{matrix} 7 & 3 \\ 4 & 6 \end{matrix}$	1 Mark	1 MIN
E	Dark	1 Mark	1 MIN
F	Dark	1 Mark	1 MIN
G	Intensity level slicing	1 Mark	1 MIN
H	Thresholding Function	1 Mark	1 MIN
I	$g(x,y) = \text{IDFT}[H(u,v)F(u,v)]$	1 Mark	1 MIN
J	Homomorphic filtering	1 Mark	1 MIN

Part B

(3Q x 5M = 15 Marks)

Q No	Solution	Scheme of Marking	Max. Time required for each Question
2.	<p>Block diagram – 2m Explanation – 2m Equations – 1m</p>  <p>FIGURE 5.1 A model of the image degradation/restoration process.</p> <p>A model of the Image Degradation/Restoration Process</p> <p>A degradation function, together with an additive noise term operates on an input image $f(x,y)$ to produce a degraded image $g(x,y)$.</p> <p>Given $g(x,y)$, some knowledge about the degradation function H and some knowledge about the additive noise term $\eta(x,y)$ we can restore an estimate $\hat{f}(x,y)$ of the original image.</p> <p>More we know about H and η the closer $\hat{f}(x,y)$ will be to $f(x,y)$.</p>  <p>If H is a linear, position-invariant process then the degraded image is given in the spatial domain by:</p> $g(x,y) = h(x,y) * f(x,y) + \eta(x,y)$ <p>Frequency Domain:</p> $G(u,v) = H(u,v) F(u,v) + N(u,v)$	2+2+1	7 MIN

↓
 Better Scan and Insert instead of Camera picture (Mobile App Cam Scanner may be used)

3.	<p>4.7.3 Summary of Steps for Filtering in the Frequency Domain</p> <p>The material in the previous two sections can be summarized as follows:</p> <ol style="list-style-type: none"> 1. Given an input image $f(x, y)$ of size $M \times N$, obtain the padding parameters P and Q from Eqs. (4.6-31) and (4.6-32). Typically, we select $P = 2M$ and $Q = 2N$. 2. Form a padded image, $f_p(x, y)$, of size $P \times Q$ by appending the necessary number of zeros to $f(x, y)$. 3. Multiply $f_p(x, y)$ by $(-1)^{x+y}$ to center its transform. 4. Compute the DFT, $F(u, v)$, of the image from step 3. 5. Generate a real, symmetric filter function, $H(u, v)$, of size $P \times Q$ with center at coordinates $(P/2, Q/2)$.[†] Form the product $G(u, v) = H(u, v)F(u, v)$ using array multiplication; that is, $G(i, k) = H(i, k)F(i, k)$. 6. Obtain the processed image: $g_p(x, y) = \left\{ \text{real} \left[\mathcal{F}^{-1} [G(u, v)] \right] \right\} (-1)^{x+y}$ <p>where the real part is selected in order to ignore parasitic complex components resulting from computational inaccuracies, and the subscript p indicates that we are dealing with padded arrays.</p> 7. Obtain the final processed result, $g(x, y)$, by extracting the $M \times N$ region from the top, left quadrant of $g_p(x, y)$. <p>Steps 1 to 4 = 0.5 mark each Steps 5 to 7 = 1 mark each</p>	5	7 MIN
4.	<p>The process of highlighting the contribution of specific bits in all pixels of an image is called bit plane slicing transformation. -1m</p> <p>Representing the images in 3 bits – 1m MSB plane – 1m Center plane – 1m LSB plane -1m</p>	1+ 4	7 MIN

(b) Bit-plane Blking

4	3	2	1
3	1	2	4
5	1	6	2
2	3	5	6

100	011	010	001
011	001	010	100
101	001	110	010
010	011	101	110

Breaking it into planes

MSB plane → Left most bit

Center plane → Central bit

LSB plane → Right most bit

1	0	0	0
0	0	0	1
1	0	1	0
0	0	1	1

MSB plane

0	1	1	0
1	0	1	0
0	0	1	1
1	1	0	1

Center bit plane

0	1	0	1
1	1	0	0
1	1	0	0
0	1	1	0

LSB plane

Part C

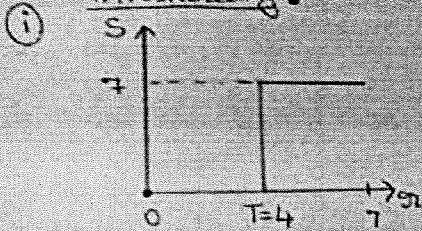
(3Qx 5M = 15 Marks)

Q No	Solution	Scheme of Marking	Max. Time required for each Question
------	----------	-------------------	--------------------------------------

5a

solⁿ: $2^3 = 8$ levels

Thresholding:



$$g(x,y) = \begin{cases} 0 & \text{if } f(x,y) < 4 \\ 7 & \text{if } f(x,y) \geq 4 \end{cases}$$

$$g(x,y) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 7 & 7 & 7 \\ 7 & 0 & 7 & 0 \\ 0 & 0 & 7 & 0 \end{bmatrix}$$

2+1.5+

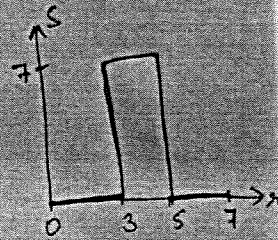
1.5

8 MIN

a) Without background

$$S = \begin{cases} (L-1) = 7 & 3 \leq x \leq 5 \\ 0 & \text{otherwise} \end{cases}$$

$$\therefore g(x,y) = \begin{bmatrix} 0 & 0 & 7 & 0 \\ 0 & 7 & 0 & 0 \\ 7 & 0 & 7 & 7 \\ 7 & 0 & 0 & 0 \end{bmatrix}$$

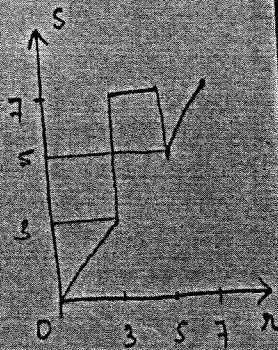


5b

b) with background

$$g(x,y) = S = \begin{cases} (L-1) = 7 & 3 \leq x \leq 5 \\ x & \text{otherwise} \end{cases}$$

$$\therefore g(x,y) = \begin{bmatrix} 1 & 2 & 7 & 0 \\ 2 & 7 & 6 & 7 \\ 7 & 2 & 7 & 7 \\ 7 & 2 & 6 & 1 \end{bmatrix}$$



Thresholding – 2m

Intensity level slicing with background – 1.5m

Intensity level slicing without background - 1.5m

6

3+1+1

8 MIN

Y_k	P_k	P_m $= P_k / T_m$	C_m	$L = 20 \times C_m$	Roundoff
1	1	0.625	0.625	1.25	1
2	3	0.1875	0.25	5	5
3	3	0.1875	0.4375	8.75	8
4	2	0.125	0.5625	11.25	11
5	2	0.125	0.6875	13.75	13
6	1	0.625	0.75	15	15
7	3	0.1875	0.9375	18.75	18
8	1	0.0625	1	20	20

$T_m = 16$

Probability (P_m)

$$P_k = \frac{\text{No. of pixels}}{\text{Total no. of pixels}}$$

C_m is Cumulative Probability

$$C_m = P_m + P_m \text{ (rest)}$$

So the original image has been transformed to the equalized image with different intensity on each pixel. Hence we see that the intensity range of the pixels have been increased & hence the histogram of the image will look more spread.

3	2	4	5	⇒	8	5	11	13
7	7	8	2		18	18	20	5
3	1	2	3		8	1	5	8
5	4	6	7		13	11	15	18

Output histogram

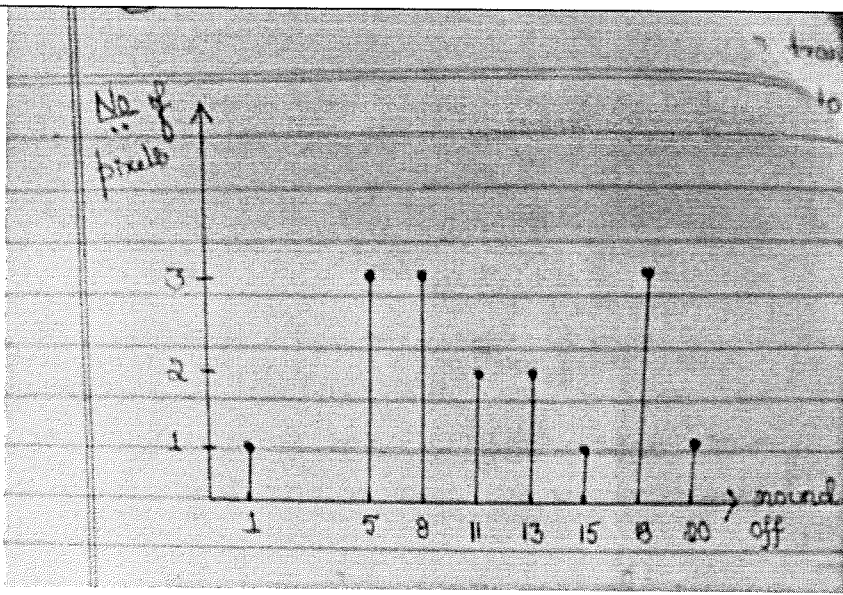
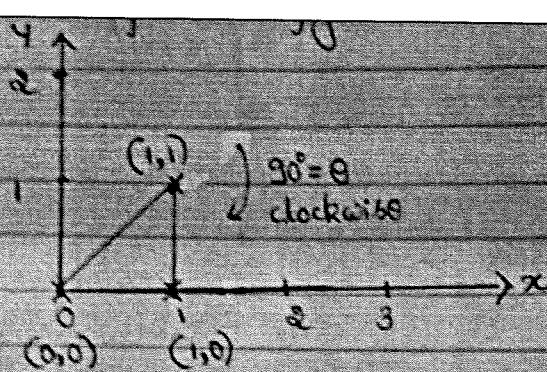


Table – 3m

Output histogram – 1m

Input image and transformed image intensities values in matrix form– 1m

7	<p>Original location of triangle with coordinates – 1m</p> <p>New transformed figure with coordinates– 1m</p> <p>For each vertices finding the new vertices - 1m each</p>	<p>1+1+1+</p> <p>1+1</p>	<p>8 MIN</p>
---	---	--------------------------	--------------



W.K.T for Rotation (clockwise):

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\begin{aligned} \sin 90 &= 1 \\ \cos 90 &= 0 \end{aligned}$$

$$\therefore \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

(i) for (0,0) & $\theta = 90^\circ$

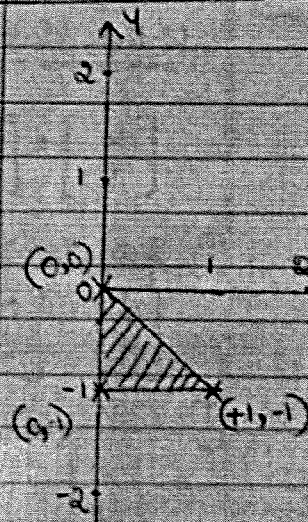
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

(ii) for (1,0) & $\theta = 90^\circ$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ -1 \end{bmatrix}$$

(iii) for (1,1) & $\theta = 90^\circ$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$





Roll No																			
---------	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--

**PRESIDENCY UNIVERSITY
BENGALURU**

SCHOOL OF ENGINEERING

END TERM FINAL EXAMINATION

Semester: Odd Semester: 2019-20

Date: 28 December 2019

Course Code: ECE 307

Time: 9:30 AM to 12:30 PM

Course Name: DIGITAL IMAGE PROCESSING

Max Marks: 80

Program & Sem: B.Tech (ECE) & V (DE-I)

Weightage: 40%

Instructions:

- (i) Read the all questions carefully and answer accordingly.
- (ii) All Questions are compulsory.

Part A [Memory Recall Questions]

Answer all the Questions. Each Question carries 1 mark. (10Qx1M=10M)

- 1. Formulate the basic form of Power law transformation? (C.O.No.2) [Knowledge]
- 2. For given 3x3 image obtain the negative transformation of an image (C.O.No.2) [Knowledge]

1	0	1
1	1	1
0	0	0

- 3. What is the process of correcting the power-law response phenomena in display devices? (C.O.No.2) [Knowledge]
- 4. Define Unitary Matrix? (C.O.No.2) [Knowledge]
- 5. Define and formulate Translation and Reflection in Morphological Image Processing? (C.O.No.4) [Knowledge]
- 6. Consider the two image segments shown by A and B. If $A = \begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ find A XOR B and A AND B (C.O.No.1) [Knowledge]
- 7. Specify the components of Digital Image Processing? (C.O.No.1) [Knowledge]
- 8. List the steps involved in Digital Image Processing? (C.O.No.1) [Knowledge]
- 9. List the steps in digitizing the continuous Image? (C.O.No.1) [Knowledge]
- 10. Define and formulate Compression Ratio? (C.O.No.3) [Knowledge]

Part B [Thought Provoking Questions]

Answer all the Questions. Each Question carries 10 marks. (3Qx10M=30M)

- 11. Define Morphology? Given an image A and structuring element B. Compute:
 - (i) A Dilated by B ($A \oplus B$) (C.O.No.4) [Comprehension]
 - (ii) A Erosion by B ($A \ominus B$)

(iii) A^c Erosion by B ($A^c \ominus B$)

A					
0	0	0	0	0	0
0	0	1	1	0	0
0	1	1	1	1	0
0	0	1	1	0	0
0	0	0	0	0	0

B
1
1
1

12. Explain how multi-resolution analysis can be done using image pyramids. With a neat block diagram explain the steps involved in for obtaining approximation and Prediction residual pyramids. (C.O.No.4) [Comprehension]
13. With neat diagrams, write a brief note on: (C.O.No.4) [Comprehension]
- I. RGB Color model
 - II. Intensity level Slicing

Part C [Problem Solving Questions]

Answer all the Questions. Each Question carries 10 marks. (4Qx10M=40M)

14. a) Let p and q are two pixels at co-ordinates (10,15) and (15,25) respectively. Compute: i) Euclidean distance ii) Chessboard distance and iii) City Block distance. And conclude which determines minimum distance.
- b) Given $f1 = \begin{bmatrix} 0 & 2 \\ 2 & 3 \end{bmatrix}$, $f2 = \begin{bmatrix} 6 & 5 \\ 4 & 7 \end{bmatrix}$, $a1=1$ $a2= -1$ and $H= \max$. Determine weather it is a Linear operation or non-Linear operation. (C.O.No.1) [Comprehension]
15. Perform histogram equalization of the following 8x8 image. The gray level distribution of the image is given below. Draw the input and output histogram. (C.O.No.2) [Comprehension]

Gray level r_k	0	1	2	3	4	5	6	7
No of pixels n_k	8	10	10	2	12	16	4	2


16. An information source produces a sequence of independent symbols having the following probabilities. Construct a binary code using Huffman encoding and find the average length of this code for the following symbols. (C.O.No.3) [Comprehension]

Symbol	s1	s2	s3	s4	s5	s6	s7
Probability	0.4	0.2	0.1	0.1	0.1	0.05	0.05

17. Given an image strip corresponds to the intensity profile, and the numbers in the boxes are the intensity values of the dots shown in the profile. Highlight the Edge, line and isolated point in the input image strip. (C.O.No.3) [Comprehension]
- (i) State the first order and second order derivative equations.
 - (ii) Draw the intensity for the image strip
 - (iii) Obtain the First Order Derivative and Second order Derivative of the image strip.

5	5	4	3	2	1	0	0	0	6	0	0	0	0	1	3	1	0	0	0	7	7	7	7	0	0
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

Reviewer Comment:

DR. M. LEVY 

Format of Answer Scheme



SCHOOL OF ENGINEERING

SOLUTION

Semester: Odd Sem. 2019-20

Date: 28.12.2019

Course Code: ECE307

Time: 3 HRS

Course Name: Digital Image Processing

Max Marks: 80

Program & Sem: SOE & 5th

Weightage: 40%

Part A

(10Q x 1M = 10Mark)

Q No	Solution	Scheme of Marking	Max. Time required for each Question									
1	$S=c.r^y$ where c = Constant and $0<r<L-1$	1	1min									
2	<table border="1" style="display: inline-table; vertical-align: middle;"> <tr> <td>0</td> <td>1</td> <td>0</td> </tr> <tr> <td>0</td> <td>0</td> <td>0</td> </tr> <tr> <td>1</td> <td>1</td> <td>1</td> </tr> </table>	0	1	0	0	0	0	1	1	1	1	1min
0	1	0										
0	0	0										
1	1	1										
3	Gamma Correction	1	1min									
4	Unitary Matrix $A^{-1} = A^{*T}$ Matrix A is called Unitary matrix if A inverse is equal to A conjugate transpose	1	1min									
5	Reflection $B' = w w = -b, \text{ for } b \in B\}$ Translation $B_z = \{c c = b + z$	1	1min									
6	$A \text{ XOR } B = \begin{bmatrix} 1 & 1 \\ 0 & 0 \end{bmatrix}$ $A \text{ AND } B = \begin{bmatrix} 0 & 0 \\ 1 & 1 \end{bmatrix}$	1	1min									
7	Image Display Computer Mass Storage Hardcopy Specialized image processing Hardware Image Processing Software Image sensor Network	1	1min									

8	Image Acquisition Image Enhancement Image Restoration Color Image Processing Wavelets and Multi-resolution analysis Compression Morphological Image processing Segmentation Representation and Description Object Recognition	1	1min
9	Sampling and Quantization	1	1min
10	Compression Ration = $\frac{\text{Original Image}}{\text{Compressed Image}}$	1	1min

Part B

(3Q x 10M = 30 Marks)

Q No	Solution	Scheme of Marking	Max. Time required for each Question
2	<p>Define Mathematical Morphology</p> <p>Morphological Image Processing is used to extract image components for representation and description of various objects, such as boundaries, skeletons and the convex hull.</p> <p>Mathematical Morphology is set theory to represent objects in an image.</p> <p>Example: (i) A Dilated by B (A ⊕ B) (ii) A Eroded by B (A ⊖ B) (iii) A ⊕ B Eroded by B (A ⊖ B)</p> <p> $A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$ $B = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$ $A^c = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 1 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 \end{bmatrix}$ </p> <p> $A \oplus B = \begin{bmatrix} 0 & 1 & 1 & 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 & 0 \end{bmatrix}$ </p> <p> $A \ominus B = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$ </p> <p> $A \ominus B = \begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 0 & 1 & 1 & 1 & 1 \end{bmatrix}$ </p>	3+2+2+3	20min

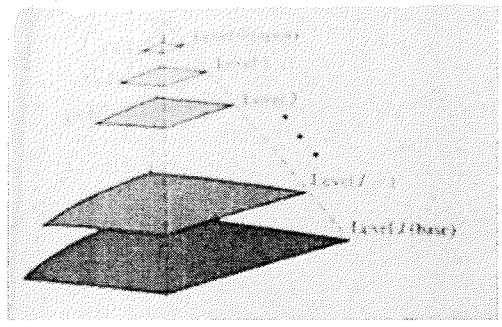
3

Let I be the original image of size $M \times N$. Let I_j be the image of size $M_j \times N_j$ at level j . The image I_j is a reduced-resolution approximation of I . The image I_j is generated by filtering and downsampling the image I_{j-1} by a factor of s . The image I_j is a reduced-resolution approximation of I . The image I_j is generated by filtering and downsampling the image I_{j-1} by a factor of s . The image I_j is a reduced-resolution approximation of I . The image I_j is generated by filtering and downsampling the image I_{j-1} by a factor of s .

3+2+3+2

20min

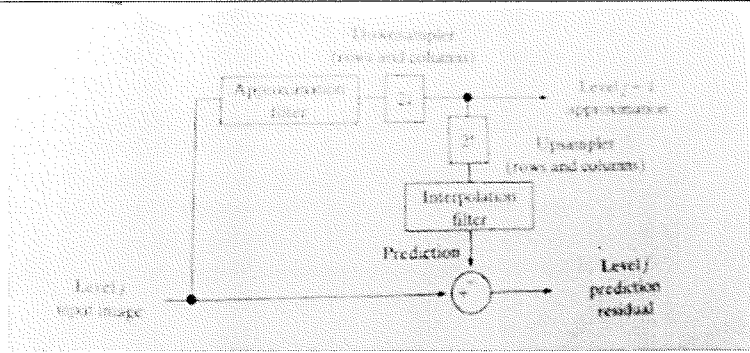
Image Pyramid Diagram



Step 1 Compute a reduced-resolution approximation of the level j input image. This is done by filtering and downsampling the input image by a factor of s . This is the resulting approximation at level $j+1$ of the approximation pyramid.

Step 2 Compute an estimate of the level j input image from the reduced-resolution approximation generated in step 1. This is done by upsampling and filtering the generated approximation. The resulting predicted image will have the same dimension as the level j input image.

Step 3 Compute the difference between the predicted image of step 2 and the input to step 1. This is the result at level j of the prediction residual pyramid.



4

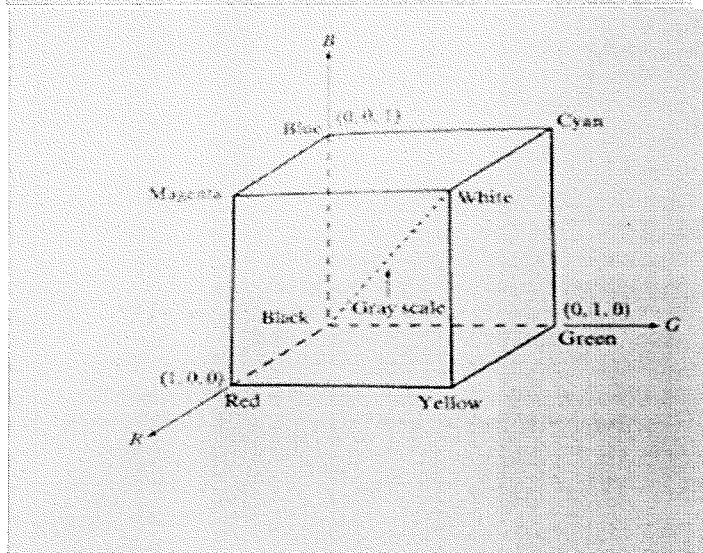
(F) RGB Color Model

(5)

In the RGB color model, each color appears as a primary spectral component of red, green and blue. This model is based on a Cartesian 3D coordinate system. The color subspace of interest is the cube in which the primary values are at three corners, the secondary color cyan, magenta, and yellow are at three other corners, black is at the origin and white is at the corner furthest from the origin. The gray scale extends from black to white along the line joining these two points. The different colors in the model are points inside the cube and are defined by vectors extending from the origin. RGB = white (level 1), so a bit RGB image = $(2^8)^3 = 2^{24}$

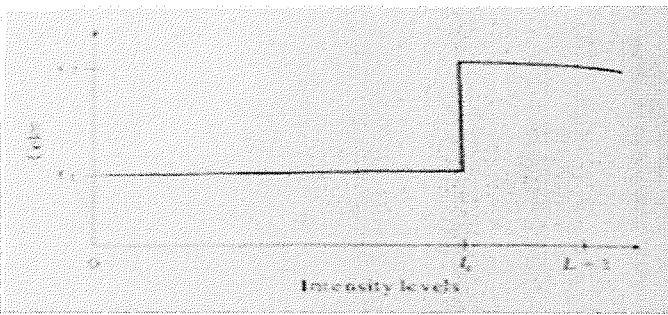
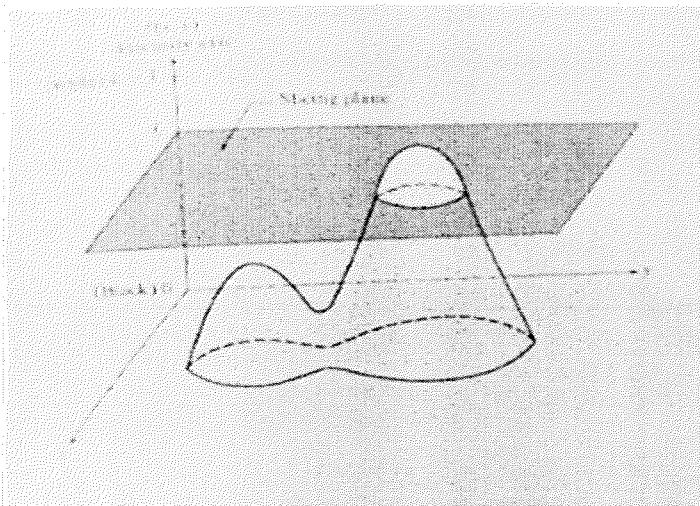
3+2+3+2

20min



The technique of intensity quantization is also an example of quantization. In general, if an image is represented as a continuous function, the method involves dividing the range of gray levels into a finite number of gray levels. Each plane, which is a function in the range of intensity, if different colors is assigned to each side of the plane, any point above plane, that is above the plane will be coded with one color, and any point below the plane will be coded with another color.

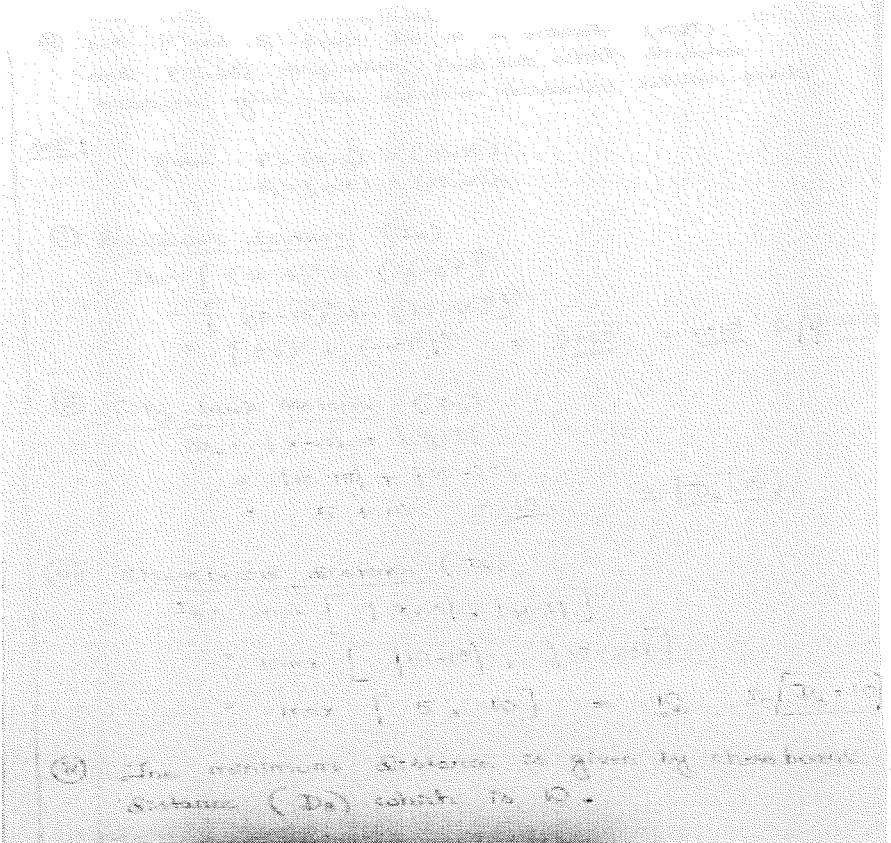
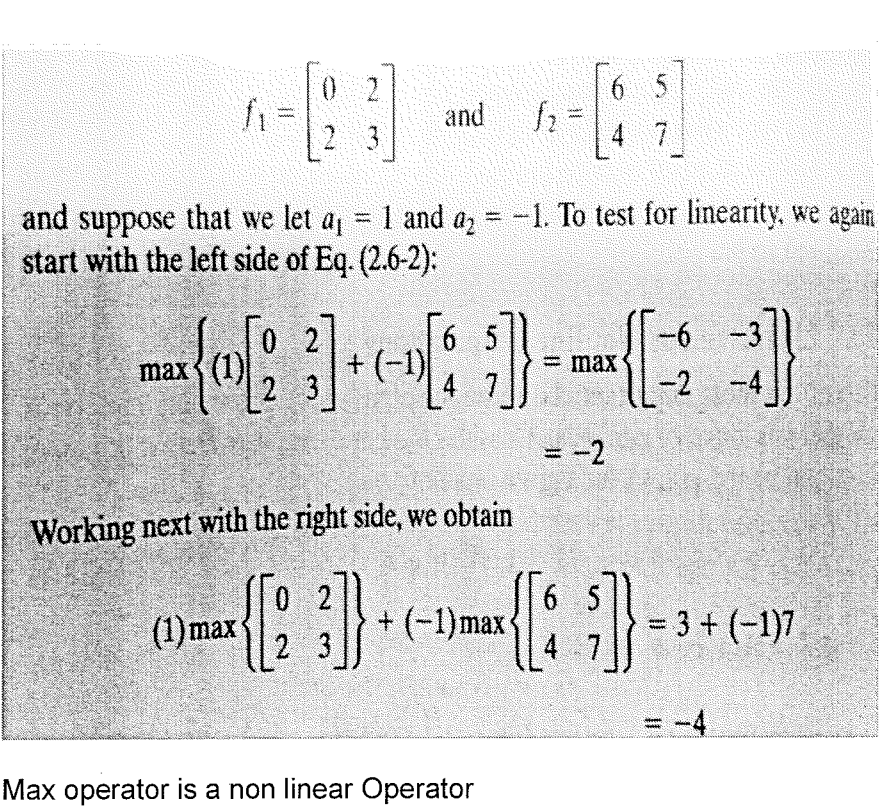
If $0 \leq I \leq 1$ represent the gray scale, but level 0 represents black $[f(I) = 0]$ and level 1 represents white $[f(I) = 1]$. Suppose that P planes perpendicular to the intensity axis as defined at levels I_1, I_2, \dots, I_{P-1} , the P planes partition the gray scale into $P+1$ intervals $I_0, I_1, \dots, I_{P-1}, I_P$ of length



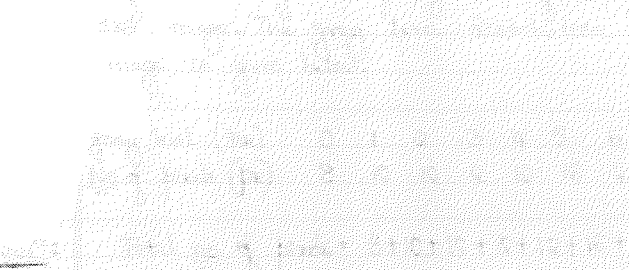
Part C

(0Q x 0M = 0Marks)

	Solution	Max. Time required
--	-----------------	---------------------------

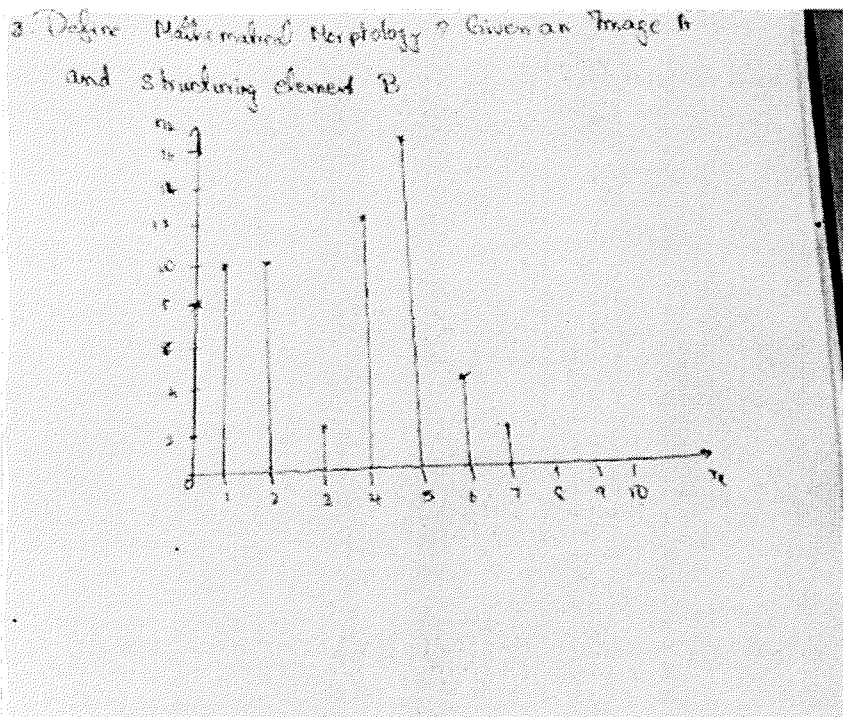
Q No		Scheme of Marking	for each Question
5a		1.5+1.5+1.5+0.5	20min
5b	 <p> $f_1 = \begin{bmatrix} 0 & 2 \\ 2 & 3 \end{bmatrix} \quad \text{and} \quad f_2 = \begin{bmatrix} 6 & 5 \\ 4 & 7 \end{bmatrix}$ </p> <p>and suppose that we let $a_1 = 1$ and $a_2 = -1$. To test for linearity, we again start with the left side of Eq. (2.6-2):</p> $\max \left\{ (1) \begin{bmatrix} 0 & 2 \\ 2 & 3 \end{bmatrix} + (-1) \begin{bmatrix} 6 & 5 \\ 4 & 7 \end{bmatrix} \right\} = \max \left\{ \begin{bmatrix} -6 & -3 \\ -2 & -4 \end{bmatrix} \right\}$ $= -2$ <p>Working next with the right side, we obtain</p> $(1) \max \left\{ \begin{bmatrix} 0 & 2 \\ 2 & 3 \end{bmatrix} \right\} + (-1) \max \left\{ \begin{bmatrix} 6 & 5 \\ 4 & 7 \end{bmatrix} \right\} = 3 + (-1)7$ $= -4$ <p>Max operator is a non linear Operator</p>	2+2+1	

Q.2. Program to calculate the histogram of an image.

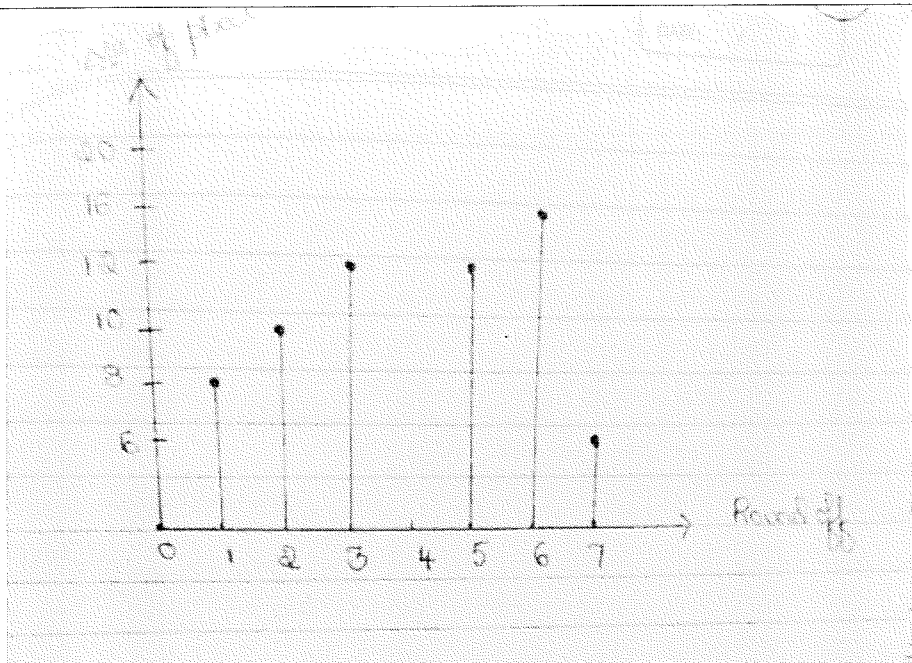
Input Image: 

x	h _x	h _{norm}	C _{norm}	h _{norm} * C _{norm}	h _{norm} * C _{norm} * L _{max}
0	1	0.0000	0.0000	0.0000	0
1	7	0.0005	0.0005	0.0005	0
2	10	0.0005	0.0005	0.0005	0
3	2	0.0005	0.0005	0.0005	0
4	12	0.0005	0.0005	0.0005	0
5	6	0.0005	0.0005	0.0005	0
6	1	0.0005	0.0005	0.0005	0
7	2	0.0005	0.0005	0.0005	0
Total					64

Input Histogram



Output Histogram



7

6+2+2

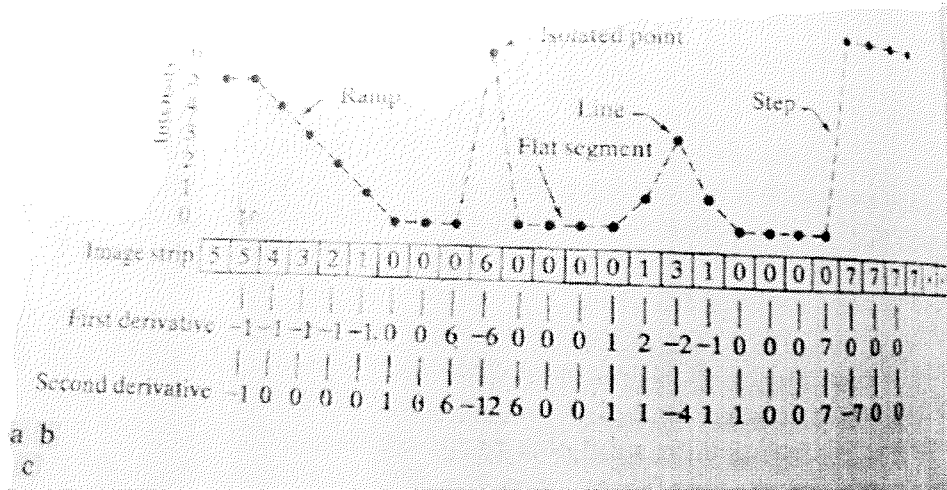
20min

Source Symbols	P_i	Code	Source S_1		Source S_2		Source S_3		Source S_4		Source S_5	
			P_i	Code	P_i	Code	P_i	Code	P_i	Code	P_i	Code
s_1	0.4	1	0.4	1	0.4	1	0.4	1	0.4	1	0.6	0
s_2	0.2	01	0.2	01	0.2	01	0.2	01	0.4	00	0.4	0
s_3	0.1	0010	0.1	0010	0.2	000	0.2	000	0.2	01		1
s_4	0.1	0011	0.1	0011	0.1	0010	0.2	001				
s_5	0.1	0000	0.1	0000	0.1	0011						
s_6	0.05	00010	0.1	0001								
s_7	0.05	00011										

Table 2.45: Code-table for example 2.27 with composite symbol placed "as low as possible"

The average length L is given by,

$$\begin{aligned}
 L &= \sum_{i=1}^7 p_i l_i \\
 &= (0.4)(1) + (0.2)(2) + (0.1)(4) + (0.1)(4) + (0.1)(4) + (0.05)(5) + (0.05)(5) \\
 &= 2.5 \text{ bits/message-symbol}
 \end{aligned}$$



First-order derivative

$$\frac{\partial f}{\partial x} = f'(x) = f(x+1) - f(x)$$

Second-order derivative

$$\frac{\partial^2 f}{\partial x^2} = f(x+1) + f(x-1) - 2f(x)$$

