



# PRESIDENCY UNIVERSITY

BENGALURU

## Mid - Term Examinations – October 2025

Date: 10-10-2025

Time: 02.00pm to 03.30pm

<b>School:</b> SOE/SOCSE	<b>Program:</b> B. Tech.	
<b>Course Code:</b> MAT2501	<b>Course Name:</b> INTEGRAL TRANSFORMS AND PARTIAL DIFFERENTIAL EQUATIONS	
<b>Semester:</b> III	<b>Max Marks:</b> 50	<b>Weightage:</b> 25%

CO - Levels	CO1	CO2	CO3	CO4	CO5
<b>Marks</b>	<b>26</b>	<b>24</b>			

### Instructions:

- (i) Read all questions carefully and answer accordingly.
- (ii) Do not write anything on the question paper other than roll number.

### Part A

Answer ALL the Questions. Each question carries 2marks.

5Q x 2M=10M

1	Find the Laplace transform of (i) $\sin 2t$ (ii) $\cosh 3t$ .	2 Marks	L1	CO1
2	Express the function $f(t) = \begin{cases} f_1(t), & 0 < t < a \\ f_2(t), & t \geq a \end{cases}$ in terms of unit step function.	2 Marks	L1	CO1
3	Find the inverse Laplace transform of i) $\frac{2}{s+3}$ ii) $\frac{s}{s^2+9}$ .	2 Marks	L1	CO1
4	Verify whether the function $f(x) = \frac{\pi-x}{2}$ defined in the interval $[0, 2\pi]$ is even or odd.	2 Marks	L1	CO2
5	Write the formula of Fourier sine series over the interval $[0, \pi]$ .	2 Marks	L1	CO2

### Part B

**Answer the Questions.**

**Total Marks 40M**

6	a	Find the Laplace transform of $\sin 3t \cos 4t$ .	5 Marks	L2	CO1
	b	Find the Laplace transform of $t^2 \sin at$ .	5 Marks	L2	CO1
<b>Or</b>					
7		Find the Laplace transform of below function by expressing it in terms of unit step function $f(t) = \begin{cases} 1, & 0 < t \leq 1 \\ t, & 1 < t \leq 2 \\ t^2, & t > 2 \end{cases}$	10 Marks	L2	CO1

8	a	Find the inverse Laplace transform of $\tan^{-1}\left(\frac{1}{s}\right)$ .	4 Marks	L3	CO1
	b	Find the inverse Laplace transform of $\frac{1}{(s^2+1)(s^2+9)}$ by using the concept of convolution theorem.	6 Marks	L3	CO1
<b>Or</b>					
9		Apply the concept of Laplace transform to solve the equation $\frac{d^2 y}{dt^2} + 4 \frac{dy}{dt} + 3y = e^{-t}$ with $y(0) = y'(0) = 0$ .	10 Marks	L3	CO1

10		Obtain the Fourier series for the function $f(x) = x + x^2$ in $[-\pi, \pi]$ .	10 Marks	L3	CO2
<b>Or</b>					
11		Find the Fourier series for $f(x) = \pi x$ in $-1 \leq x \leq 1$ and hence deduce that $\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots$ .	10 Marks	L3	CO2

12	Obtain half range Fourier sine series of $f(x)=x$ in $(0, \pi)$ and hence deduce that $\frac{\pi}{4}=1-\frac{1}{3}+\frac{1}{5}-\frac{1}{7}+....$	10 Marks	L3	CO2														
Or																		
13	Find Fourier series of $y$ in $(0,6]$ up to second harmonic for the following data <table><tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td></tr><tr><td>y</td><td>4</td><td>8</td><td>15</td><td>7</td><td>6</td><td>2</td></tr></table>	x	0	1	2	3	4	5	y	4	8	15	7	6	2	10 Marks	L3	CO2
x	0	1	2	3	4	5												
y	4	8	15	7	6	2												