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# SCHOOL OF ENGINEERING <br> END TERM EXAMINATION - FEB 2023 

Semester: Semester I-2022
Course Code : MAT1003
Course Name : Sem I - MAT1003-Applied Statistics
Program : B. Tech - (All Programs)

Date : 23-FEB-2023
Time : 9.30AM - 12.30PM
Max Marks: 100
Weightage : 50\%

## Instructions:

(i) Read all questions carefully and answer accordingly.
(ii) Question paper consists of 3 parts.
(iii) Scientific and non-programmable calculator are permitted.
(iv) Do not write any information on the question paper other than Roll Number.

## PART A

## ANSWER ALL THE QUESTIONS

(10 X $2=20 \mathrm{M}$ )

1. Give the formula for Arithmetic mean for unclassified data.
(CO1) [Knowledge]
2. Find the position of upper quartile $Q_{3}$ for the following data set: $25,27,199,29,432,100,87,76,86,34$, 123.
(CO1) [Knowledge]
3. Write the variance formula for the population.
(CO1) [Knowledge]
4. If the coefficient of correlation is $r=1$, then the correlation is called ?
(CO1) [Knowledge]
5. If a certain linear regression equation is found to be $2 x+3=5 y$, calculate the regression coefficient of $x$ on $y$.
(CO1) [Knowledge]
6. Two dice are thrown simultaneously. Find the probability of getting the same number on both dice?
(CO2) [Knowledge]
7. What are the simple events for the given set $\mathrm{H}=\{1,2,3,4\}$ ?
(CO2) [Knowledge]
8. While considering the conditional probability $P(B \mid A)$, which event has occurred first, A or B ?
(CO2) [Knowledge]
9. If the random variable $X$ follows the Poisson distribution with $\lambda=4$, then find the value of $P(X=6)$
(CO3) [Knowledge]
10. State the probability mass function for a Binomial distribution.
(CO3) [Knowledge]

## PART B

## ANSWER ALL THE QUESTIONS

( $5 \times 10=50 \mathrm{M}$ )
11. Following are the marks obtained by a student $B$ in 10 tests of 100 marks each
$\left[\begin{array}{ccccccccccc}\text { Test } & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \text { Marks obtained by } & \text { B } & 48 & 75 & 54 & 60 & 63 & 69 & 72 & 51 & 57 \\ 66\end{array}\right]$

Determine the standard deviation of marks.
(CO1) [Comprehension]
12. Police plan to enforce speed limits by using radar traps at 3 different locations within the city limits. The radar traps at each of the locations P, Q and R are operated $40 \%, 30 \%$ and $20 \%$ of the time. A person who is speeding on her way to work has probabilities of $0.2,0.1$ and 0.5 respectively, of passing through these locations. If the person received a speeding ticket on her way to work, what is the probability that she passed through the radar trap located at (i) location $P$ (ii) location $R$ ?
(CO2) [Comprehension]
13. Compute Karl Pearson's coefficient of correlation between capital employed and profit obtained from the following data

| Capital Employed (Rs. In Crore) | 10 | 20 | 30 | 40 | 50 | 60 | 70 | 80 | 90 | 100 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Profit (Rs in Crore) | 2 | 4 | 8 | 5 | 10 | 15 | 14 | 20 | 22 | 50 |

Also determine the nature of correlation of the observation.
(CO1) [Comprehension]
14. It has been observed that 10 drops of water trickle every 5 minutes from a leaking pipe. What is the probability that in 5 minutes (a) at least 2 drops of water trickle (b) at most 2 drops of water trickle (c) exactly 6 drops of water trickle?
(CO3) [Comprehension]
15. Salaries of employees of a certain organization are normally distributed with a mean of 7 LPA and standard deviation of 3 LPA. What is the probability that, for a randomly selected employee of this organization, the salary would be
(a) at least 5 LPA
(b) at most 5 LPA
(c) between 6 and 8 LPA
(Given that $P(Z \leq 0.33)=0.62930, P(Z \leq 0.67)=0.74857)$.
(CO3) [Comprehension]

## PART C

## ANSWER ALL THE QUESTIONS

( $2 \times 15=30 \mathrm{M}$ )
16. Consider the following data set:

$$
\begin{array}{lllllllllll}
\hline \text { Marks in Subject P } 10 & 13 & 14 & 16 & 11 & 18 & 10 & 12 & 20 & 18 \\
\hline \text { Marks in Subject Q } 13 & 12 & 18 & 15 & 17 & 15 & 11 & 14 & 10 & 16 \\
\hline
\end{array}
$$

Construct suitable mathematical models to estimate:
a. Marks in Subject $P$ when marks in Subject $Q$ is known
b. Marks in Subject $Q$ when marks in Subject $P$ is known
(CO1) [Application]
17. It has been observed that 1 out of 8 bulbs manufactured by a factory are defective.
a. Construct a suitable mathematical model, which represents the number of defective bulbs manufactured by the factory out of a total of $n$ bulbs.
b. If a box of 10 bulbs is selected, what is the probability that at most 2 are defective?
c. If a box containing 9 bulbs is selected, what is the probability that more than 8 are defective?
d. If 50 bulbs are picked up, what is the mean number of defective bulbs?
(CO3) [Application]

