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# PRESIDENCY UNIVERSITY **BENGALURU**

# SCHOOL OF ENGINEERING **MID TERM EXAMINATION - APR 2023**

**Date:** 15-APR-2023 **Semester:** Semester II - B.Tech MATH - 2022

Course Code: MAT2003 Time: 2:00PM - 3:30PM

Course Name: Sem IV - MAT2003 - Numerical Methods for Engineers Max Marks: 50

Program: Mathematics for B.Tech Weightage: 25%

#### Instructions:

(i) Read all questions carefully and answer accordingly.

(ii) Question paper consists of 3 parts.

(iii) Scientific and non-programmable calculator are permitted.

(iv) Do not write any information on the question paper other than Roll Number.

#### **PART A**

### **ANSWER ALL THE QUESTIONS**

(5 X 2 = 10M)

**1.** State the elements  $u_{12}$  and  $u_{13}$  from  $\begin{bmatrix} 1 & 4 & -3 \\ -2 & 8 & 5 \\ 3 & 4 & 7 \end{bmatrix}$ .

(CO1) [Knowledge]

2. State the second approximation of Gauss Siedel method for the system of equations,  $a_{11}x + a_{12}y + a_{13}z = b_1, a_{21}x + a_{22}y + a_{23}z = b_2, a_{31}x + a_{32}y + a_{33}z = b_3.$ 

(CO1) [Knowledge]

3. Recognize the interval in which root of the equation lies, from the following data f(0)=-1, f(1)=-0.5, f(2)=-0.1, f(3)=0.5, f(4)=1.5

(CO1) [Knowledge]

**4.** From the given data set find  $\Delta f_0$ 

x	0	0.1	0.2	0.3
f(x)	5	12	27	41

(CO2) [Knowledge]

**5.** If  $f(x_0) = y_0$ ,  $f(x_1) = y_1$  and  $f(x_2) = y_2$ , then the Newton's divided difference second order polynomial for the above data is given by

$$P_2(x) = b_0 + b_1(x - x_0) + b_2(x - x_0)(x - x_1)$$
  
. Identify  $b_0$ .

(CO2) [Knowledge]

#### **PART B**

## **ANSWER ALL THE QUESTIONS**

(4 X 7 = 28M)

**6.** Estimate the elements L and U matrices from the following system of equation x+y+z=1; 4x+3y-z=6; 3x+5y+3z=4

(CO1) [Comprehension]

7. Identify the real root of the equation  $xe^x - 2 = 0$  correct to three decimal places. Carry out 3 decimal places

(CO1) [Comprehension]

**8.** For the following data, predict y at x=19.4 using appropriate formula.

X	19	20	21	22	23	
Υ	91	100.25	110	120.25	131	

(CO2) [Comprehension]

**9.** Predict y(10) using the appropriate interpolation formula from the table given below:

x:	5	6	9	11
y:	12	13	14	16

(CO2) [Comprehension]

#### **PART C**

# **ANSWER THE FOLLOWING QUESTION**

 $(1 \times 12 = 12M)$ 

**10.** From Gauss Seidel iteration method solve the system of equations 5x + 2y + z = 12, x + 4y - 2z = 15, x + 2y + 5z = 20. Carry out four iterations.

(CO1) [Application]