## PRESIDENCY UNIVERSITY BENGALURU

## SCHOOL OF ENGINEERING <br> MID TERM EXAMINATION - APR 2023

Semester : Semester II - B.Tech MATH - 2022
Date : 15-APR-2023
Course Code : MAT2003
Course Name : Sem IV - MAT2003 - Numerical Methods for Engineers
Program : Mathematics for B.Tech

Time : 2:00PM - 3:30PM
Max Marks : 50
Weightage : 25\%

## Instructions:

(i) Read all questions carefully and answer accordingly.
(ii) Question paper consists of 3 parts.
(iii) Scientific and non-programmable calculator are permitted.
(iv) Do not write any information on the question paper other than Roll Number.

## PART A

## ANSWER ALL THE QUESTIONS

1. State the elements $u_{12}$ and $u_{13}$ from $\left[\begin{array}{ccc}1 & 4 & -3 \\ -2 & 8 & 5 \\ 3 & 4 & 7\end{array}\right]$.
(CO1) [Knowledge]
2. State the second approximation of Gauss Siedel method for the system of equations, $a_{11} x+a_{12} y+a_{13} z=b_{1}, a_{21} x+a_{22} y+a_{23} z=b_{2}, a_{31} x+a_{32} y+a_{33} z=b_{3}$.
(CO1) [Knowledge]
3. Recognize the interval in which root of the equation $\qquad$ lies, from the following data $f(0)=-1$, $f(1)=-0.5, f(2)=-0.1, f(3)=0.5, f(4)=1.5$
(CO1) [Knowledge]
4. From the given data set find $\Delta f_{0}$

| $x$ | 0 | 0.1 | 0.2 | 0.3 |
| :--- | :--- | :--- | :--- | :--- |
| $f(x)$ | 5 | 12 | 27 | 41 |

(CO2) [Knowledge]
5. If $f\left(x_{0}\right)=y_{0}, f\left(x_{1}\right)=y_{1}$ and $f\left(x_{2}\right)=y_{2}$, then the Newton's divided difference second order polynomial for the above data is given by
$P_{2}(x)=b_{0}+b_{1}\left(x-x_{0}\right)+b_{2}\left(x-x_{0}\right)\left(x-x_{1}\right)$
. Identify $b_{0}$.

## PART B

## ANSWER ALL THE QUESTIONS

(4 X $7=28 \mathrm{M}$ )
6. Estimate the elements $\underset{x+y+z=1 ; 4 x+3 y-z=6 ; 3 x+5 y+3 z=4}{\mathrm{~L}} \mathrm{U}$ matrices from the following system of equation (CO1) [Comprehension]
7. Identify the real root of the equation $x e^{x}-2=0$ correct to three decimal places. Carry out 3 decimal places
(CO1) [Comprehension]
8. For the following data, predict y at $\mathrm{x}=19.4$ using appropriate formula.

| X | 19 | 20 | 21 | 22 | 23 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Y | 91 | 100.25 | 110 | 120.25 | 131 |

(CO2) [Comprehension]
9. Predict $y(10)$ using the appropriate interpolation formula from the table given below:

| $\mathrm{x}:$ | 5 | 6 | 9 | 11 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{y}:$ | 12 | 13 | 14 | 16 |

(CO2) [Comprehension]

## PART C

## ANSWER THE FOLLOWING QUESTION

( $1 \times 12=12 \mathrm{M})$
10. From Gauss Seidel iteration method solve the system of equations $5 x+2 y+z=12, x+4 y-2 z=15, x+2 y+5 z=20$. Carry out four iterations.

