## PRESIDENCY UNIVERSITY BENGALURU

## SCHOOL OF ENGINEERING <br> END TERM EXAMINATION - JUN 2023

Semester: Semester II - 2022
Course Code : MAT1003
Course Name : Sem II - MAT1003 - Applied Statistics
Program : B.Tech - All Programs

Date : 7-JUN-2023
Time : 1.00PM - 4.00PM
Max Marks : 100
Weightage : 50\%

## Instructions:

(i) Read all questions carefully and answer accordingly.
(ii) Question paper consists of 3 parts.
(iii) Scientific and non-programmable calculator are permitted.
(iv) Do not write any information on the question paper other than Roll Number.

## PART A

## ANSWER ALL THE QUESTIONS

(10 X 2 = 20M)

1. Identify the arithmetic mean of the first 7 natural numbers.
(CO1) [Knowledge]
2. The probability that the Indian industry will locate in London,United Kingdom is 0.6 , the probability that it will locate in Birmingham ,United Kingdom is 0.3 , and the probability that it will locate in either London or Birmingham is 0.7 . List the probability that the industry will locate in both cities?
(CO2) [Knowledge]
3. For a singing competition 10 participants were given marks by 2 judges. The correlation co-efficient $r_{x y}$ was found to be 0.113 . Recognize the nature of correlation and describe the same.
(CO1) [Knowledge]
4. Define the shape of the normal curve.
(CO3) [Knowledge]
5. If variance of an unclassified data set is found to be 10.21 , then identify the standard deviation of that dataset.
(CO1) [Knowledge]
6. If the random variable $X$ follows the Poisson distribution with mean 2. Identify the value of $P(X=3)$.
(CO3) [Knowledge]
7. Label the probability of getting a prime number when a die is rolled once.
8. List the probability distribution for the random variable $X=$ number of tails, when three coins are tossed together.
(CO3) [Knowledge]
9. List the upper quartile for the following set of numbers: $10,50,30,20,10,20,70,30$.
(CO1) [Knowledge]
10. State the conditional probability $P(A \mid B)$ when $A$ and $B$ are independent events.
(CO2) [Knowledge]

## PART B

## ANSWER ALL THE QUESTIONS

$(5 \times 10=50 M)$
11. It is estimated that $50 \%$ of emails are spam emails. Some software has been applied to filter these spam emails before they reach your inbox. A certain brand of software claims that it can detect $99 \%$ of spam emails, and the probability of a false positive (a non-spam email detected as spam) is $5 \%$. Now if an email is detected as spam, then predict the probability that
(a) it is in fact a non-spam email?
(b) it is in fact spam email?
(CO2) [Comprehension]
12. Consider the run scored by 2 players $X$ and $Y$ in 10 consecutive overs when facing spin bowling on a scale of 0-10

| Overs | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Player X | 8 | 9 | 8 | 7 | 6 | 10 | 0 | 2 | 9 | 4 |
| Player $Y$ | 7 | 7 | 9 | 6 | 8 | 2 | 6 | 8 | 3 | 1 |

Identify the nature of the correlation prevalent between the scores of the players while facing a spinner.
(CO1) [Comprehension]
13. Suppose a card is drawn randomly from a standard deck of 52 playing cards. Predict the probability that
a) the card is a club, knowing that the card is a king?
b) the card is a spade, knowing that the card is black?
(CO2) [Comprehension]
14. Consider the following two data sets.

Data Set I: 12, 25, 37, 8, 41.
Data Set II: 19, 32, 44, 15, 48.
Estimate the standard deviation for each of these two data sets and find which set is more consistent.
(CO1) [Comprehension]
15. Salaries of employees of a certain organization are normally distributed with a mean of 7 LPA and a standard deviation of 3 LPA. Predict the probability for a randomly selected employee of this organization, the salary would be
(a) at least 5 LPA
(b) between 6 and 8 LPA
(c) at most 5 LPA.
(Given that $P(Z \leq 0.33)=0.62930, P(Z \leq 0.67)=0.74857)$.
(CO3) [Comprehension]

## PART C

## ANSWER ALL THE QUESTIONS

16. The following data gives the age of husband $(x)$ and the age of wife $(y)$ in years. Compute the two regrssion lines and calculate the age of husband corresponding to 16 years age of wife.

| x | 36 | 23 | 27 | 28 | 28 | 29 | 30 | 31 | 33 | 35 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| y | 29 | 18 | 20 | 22 | 27 | 21 | 29 | 27 | 29 | 28 |

(CO1) [Application]
17. If 2 out of 10 industrial accidents are due to fatigue, compute the probability that (a) exactly 2 out of 8 industrial accidents are due to fatigue (b) at least 2 out of 8 industrial accidents are due to fatigue (c) at most 2 out of 8 industrial accidents are due to fatigue (d) none of the 8 accidents is due to fatigue (e) all the 8 accidents are due to fatigue.

