

I D NO.

PRESIDENCY UNIVERSITY, BENGALURU

SCHOOL OF ENGINEERING

Weightage: 40 %

Max Marks: 80 Max Time: 2 hrs. 07 May 2018, Monday

ENDTERM FINAL EXAMINATION MAY 2018

Even Semester 2017-18

Course: MAT 102 Engineering Mathematics – II II Sem. All Branches

Instructions:

- *(i)* Read the question properly and answer accordingly.
- (ii) Question paper consists of 3 parts.
- (iii) Scientific and Non-programmable calculators are permitted.
- *(iv)* In Part C, answer any <u>**TWO**</u> questions.

Part A

(4 Q x 5 M = 20 Marks) 1. Form the partial differential equation from the relation $z = a \log(x^2 + y^2) + b$, by

eliminating the arbitrary constants **a** and **b**.

2. Solve
$$\frac{\partial^2 z}{\partial x^2} + z = 0$$
 given that $z = e^y$ and $\frac{\partial z}{\partial x} = 1$ at $x = 0$.

3. Find
$$L\left[e^{-4t}t^{\frac{5}{2}}\right]$$
.
4. Find $L^{-1}\left[\frac{2s-5}{s^2+25}+\frac{4}{9-s^2}+\frac{5}{3s-9}\right]$

Part B

 $(3 Q \times 10 M = 30 Marks)$

5. Solve
$$\frac{\partial^2 z}{\partial x \partial y} = e^{-y} \cos x$$
, given that $z = 0$ at $y = 0$ and $\frac{\partial z}{\partial y} = 0$ at $x = 0$.

6. If $f(t) = t^2$, 0 < t < 2 and f(t+2) = f(t) for t > 2, then find L[f(t)].

7. Using Convolution theorem, find $L^{-1}\left[\frac{1}{(s-1)(s^2+1)}\right]$.

Part C (Answer any <u>TWO</u> questions)

 $(2Q \times 15 M = 30 Marks)$

8. Express $f(t) = \begin{cases} \cos t, 0 < t < \pi \\ \cos 2t, \pi < t < 2\pi \end{cases}$ in terms of Heaviside unit step function and hence $\cos 3t, t > 2\pi$

find the Laplace transform.

9. Solve the DE
$$\frac{d^2y}{dt^2} - 2\frac{dy}{dt} + y = e^{2t}$$
 with $y(0) = 0$; $y'(0) = -1$ using Laplace

transform method.

10. (a) Evaluate
$$\int_{0}^{\infty} te^{-3t} \cos 2t dt$$
 using Laplace transform.
(b) Find $L^{-1}\left[\frac{2s-1}{s^2+4s+29}\right]$.

PRESIDENCY UNIVERSITY, BENGALURU

SCHOOL OF ENGINEERING

Weightage: 20%

Max Marks: 40

Max Time: 1 hr.

ID NO:

29 March Thursday 2018

TEST – 2

SET A

Even Semester 2017-18 Course: MAT 102 Engineering Mathematics - II II Sem All Branches

Instructions:

- (i) Read the question properly and answer accordingly.
- (ii) Question paper consists of 3 parts.
- (iii) Scientific and Non-programmable calculators are permitted.

Part A

1. Solve $\frac{d^3y}{dx^3} + 6\frac{d^2y}{dx^2} + 11\frac{dy}{dx} + 6y = 0.$

2. Solve
$$\frac{d^2 y}{dx^2} + 4 \frac{dy}{dx} + 4y = 2^x$$
.

3. Solve
$$(D^2 + 4)y = \sin 2x$$
.

Part B

(3 Q x 4 M = 12 Marks)

(2 Q x 8 M = 16 Marks)

- 4. Solve $\frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = 2x + x^2$
- 5. Solve $(D^2 2D + 5)y = e^{2x} \sin x$

Part C

(1Q x 12 M = 12 Marks)

6. Solve $\frac{d^2 y}{dx^2} - 2\frac{dy}{dx} + y = e^x \log x$ by the method of variation of parameters.

(OR)

Solve
$$(2x+1)^2 \frac{d^2 y}{dx^2} - 6(2x+1)\frac{dy}{dx} + 16y = 8(2x+1)^2$$

Page **1** of **1**

ID NO:

PRESIDENCY UNIVERSITY, BENGALURU

SCHOOL OF ENGINEERING

Weightage: 20 %

Max Marks: 40

Max Time: 1 hr.

19 Feb Monday 2018

TEST – 1

Even Semester 2017-18 Course: MAT 102 Engineering Mathematics – II All Branches

Instructions:

- (i) Read the question properly and answer accordingly.
- (ii) Question paper consists of 3 parts.
- (iii) Scientific and Non-programmable calculators are permitted.

Part A

(3 Q x 4 M = 12 Marks)

- 1. Evaluate $\int_0^a \int_0^b (x^2 + y^2) dy dx$.
- 2. Evaluate the integral $\int_0^{\pi/2} \sin^4 \theta \cos^3 \theta \, d\theta$ by expressing in terms of gamma function.
- 3. Evaluate $\int_{0}^{\infty} \int_{0}^{\infty} e^{-(x^2+y^2)} dx dy$ by changing into polar coordinates.

Part B

(2 Q x 8 M = 16 Marks)

- 4. Find by double integration the area enclosed by the curve $r=a(1+\cos\theta)$ between $\theta=0$ and $\theta=\pi$.
- 5. Evaluate $\iint_C (yz\hat{i} + zxj + xyk) \cdot \hat{n}dS$ where S is the surface of the sphere $x^2 + y^2 + z^2 = a^2$ in the first octant.

Part C

(1Q x 12 M = 12 Marks)

6. Verify Green's theorem in the *xy*-plane for $\int_C (xy+y^2)dx+x^2dy$, where C is the closed curve of the region bounded by y=x and $y=x^2$.

(OR)

Prove that $\int_{0}^{1} \frac{x^2 dx}{\sqrt{1-x^4}} \times \int_{0}^{1} \frac{dx}{\sqrt{1+x^4}} = \frac{\pi}{4\sqrt{2}}.$

