

## PRESIDENCY UNIVERSITY BENGALURU

### Department of Research & Development

#### Mid - Term Examinations - August 2024

**Odd Semester:** Ph.D. Course Work

**Course Code:** MEC 801

**Course Name:** Computational fluid dynamics

**Department:** Mechanical Engineering

**Date:** 12-08-2024

**Time:** 09.30am to 11.00am

**Max Marks:** 50

**Weightage:** 25%

#### Instructions:

- (i) Read all questions carefully and answer accordingly.
- (ii) Make suitable assumptions wherever required with justification.
- (iii) **Books, notes and data handbooks are allowed.**

1. In the context of incompressible fluid flow, consider the simplified non-dimensional transport equation:

$$u \frac{\partial u}{\partial x} = \frac{1}{Re} \frac{\partial^2 u}{\partial x^2}$$

Where  $Re$  is the Reynolds number.

Provide a detailed explanation of why, in laminar flow conditions, the diffusion term (right-hand side) tends to dominate over the convective term (left-hand side). Contrast this with highly turbulent flow conditions, where the convective term becomes more significant. Discuss the implications of these dynamics in terms of flow stability and energy dissipation.

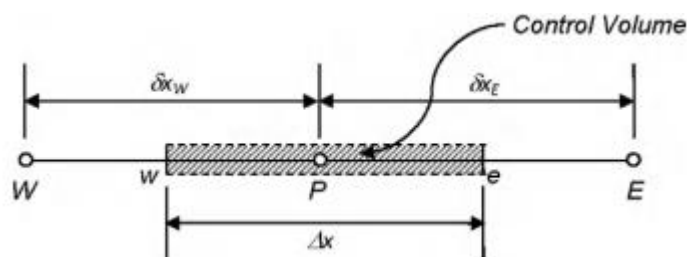
**[30 M]**

(CO:01 BL: Analyze)

2. Consider the one-dimensional steady-state diffusion term  $\frac{\partial}{\partial x} \left( G \frac{\partial \phi}{\partial x} \right)$  in the context of a control volume. Demonstrate how this term is discretized to obtain the discretized equation at a central grid nodal point P, expressed as:

$$G \frac{\partial \phi}{\partial x} \Big|_e A_E - G \frac{\partial \phi}{\partial x} \Big|_w A_w$$

where  $A_E$  and  $A_w$  are the areas associated with the east and west faces of the control volume, respectively. Discuss the implications of this discretization approach on the accuracy and stability of numerical solutions.



**[20 M]**

(CO:02 BL: Analyze)